

**THE UNIVERSITY OF HONG KONG  
FACULTY OF BUSINESS AND ECONOMICS  
School of Economics and Finance**

**FINA0402/ FINA3350 – Mathematical Finance**

**GENERAL INFORMATION**

Instructor: Dr. Rujing Meng

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Office: Room 922 K K Leung Building

Phone: 2859-1048

Consultation times: TBA and by appointments

Semester: 2

Lecture: TBA

Tutor: TBA

Pre-requisites: FINA0301/FINA2322 Derivatives

Co-requisites: /

Mutually exclusive: MATH2906/MATH3906 Financial calculus

Course Website:

Other important details:

**Course Description**

This course provides students with the necessary mathematical techniques used in continuous-time finance. It covers stochastic calculus, partial differential equation and applied probability. After taking this course, one should be able to fully understand no-arbitrage theory, the Black-Scholes equation, risk-neutral probability and martingales. The purpose of this course is to lay down a solid mathematical foundation for students to learn more advanced topics in financial engineering and risk management, such as exotic options, interest rate derivatives and credit risk models.

**COURSE OBJECTIVES**

1. to fully understand no-arbitrage theory, risk-neutral probability, martingale, and Black-Scholes equation
2. to lay down a solid mathematical foundation for students to learn more advanced topics in financial engineering and risk management, such as exotic options, interest rate derivatives and credit risk models

**FACULTY GOALS**

Goal 1: Acquisition and internalization of knowledge of the programme discipline

Goal 2: Application and integration of knowledge

Goal 3: Inculcating professionalism and leadership

Goal 4: Developing global outlook

Goal 5: Mastering communication skills

Goal 6: Cultivating leadership

**COURSE LEARNING OUTCOMES**

Course Learning Outcomes

Aligned  
Learning Outcomes

CLO1 Understand the concept and properties of a standard Brownian motion. Be able to derive probability distribution of a function of Brownian motion.	Goal 1, Goal 2
CLO2 Understand stock price model with a lognormal process. Understand the Ito's Lemma. Be able to derive a process for option price by using the Ito's Lemma.	Goal 1, Goal 2
CLO3 Understand the concept of martingale. Be able to justify whether a process is a martingale or not.	Goal 1, Goal 2
CLO4 Be able to price an option using risk-neutral probability approach.	Goal 1, Goal 2, Goal 4
CLO5 Understand no-arbitrage principle. Be able to derive put-call parity, forward price formula, and the Black-Scholes equation by using the no-arbitrage principle.	Goal 1, Goal 2
CLO6 Understand heat equation and Green's function. Be able to solve the Black-Scholes equation with an arbitrary payoff.	Goal 1, Goal 2, Goal 4
CLO7 Memorize the Black-Scholes formula. Be able to derive Greek letters from the Black-Scholes formula. Understand the asymptotic behavior of the Black-Scholes formula.	Goal 1, Goal 2

**COURSE TEACHING AND LEARNING ACTIVITIES**

Course Teaching and Learning Activities	Expected contact hour	Study Load (% of study)
T&L1. Lecture	36 hours	30%
T&L2. Tutorial	12 hours	10%
T&L3. Self-study	72 hours	60%
Total	120 hours	100%

Assessment Methods	Brief Description (Optional)	Weight	Aligned Course Learning Outcomes
A1. Assignments		30%	CLO1 – 7
A2. Exams		60%	CLO1 – 7
A3. Class/Tutorial participation		10%	CLO1 – 7
	Total	100%	

**STANDARDS FOR ASSESSMENT**

**Course Grade Descriptors**

A+, A, A-	Students demonstrate very good to excellent performance in the defined assessment criteria.
B+, B, B-	Students demonstrate good to very good performance in the defined assessment criteria.
C+, C, C-	Students demonstrate fair to good performance in the defined assessment criteria.
D+, D	Students demonstrate fair performance in the defined assessment criteria.
F	Students fail to show understanding of core materials in this course.

**Assessment Rubrics for Each Assessment**

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Assessment for each course component is consistent with the course grade descriptors listed above.

### **COURSE CONTENT AND TENTATIVE TEACHING SCHEDULE**

Lecture 1: Introduction and lattice model I  
Lecture 2: Lattice model II  
Lecture 3: Review of probability  
Lecture 4: Stochastic differential equations  
Lecture 5: Martingale approach I  
Lecture 6: Martingale approach II  
Lecture 7: Partial differential equation approach I  
Lecture 8: Partial differential equation approach II  
Lecture 9: Asymptotic analysis  
Lecture 10: Deriving and hedging with Greeks

### **REQUIRED/RECOMMENDED READINGS & ONLINE MATERIALS (e.g. journals, textbooks, website addresses etc.)**

#### **Reference books**

- Baxter, Martin, and Andrew Rennie, 1996, Financial calculus: an introduction to derivative pricing, Cambridge University Press.
- Buchanan, J. Robert, 2008, An undergraduate introduction to financial mathematics, 2nd edition, NJ : World Scientific Publishing Company.
- Hull, John, 2011, Options, Futures, & Other Derivatives, 8<sup>th</sup> edition, Prentice Hall.

### **MEANS/PROCESSES FOR STUDENT FEEDBACK ON COURSE**

- conducting mid-term survey in additional to SETL around the end of the semester
- Online response via Moodle site
- Others: Course Evaluation at the end of the course (please specify)

### **COURSE POLICY (e.g. plagiarism, academic honesty, attendance, etc.)**

The University Regulations on academic dishonesty will be strictly enforced! Please check the University Statement on plagiarism on the web: <http://www.hku.hk/plagiarism/>

### **ADDITIONAL COURSE INFORMATION (e.g. e-learning platforms & materials, penalty for late assignments, etc.)**